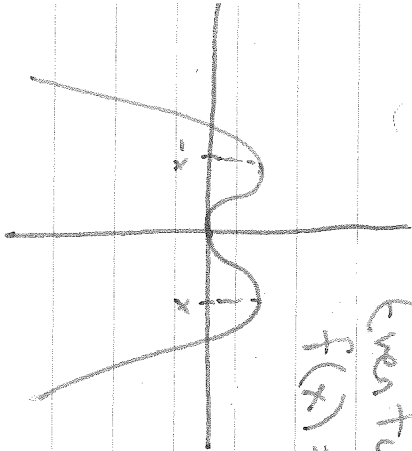


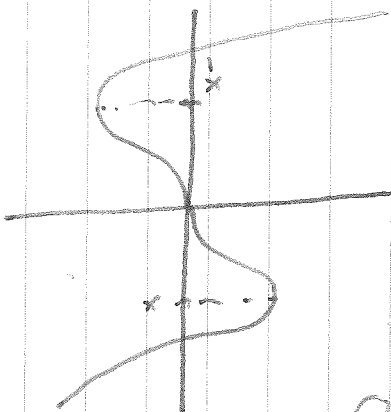
Even function

$$f(x) = f(-x)$$



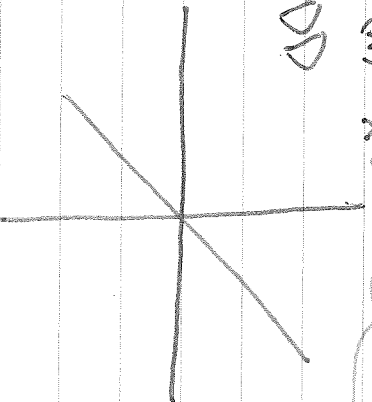
Odd function

$$f(x) = -f(-x)$$



Ex: $f(x) = x$

ODD



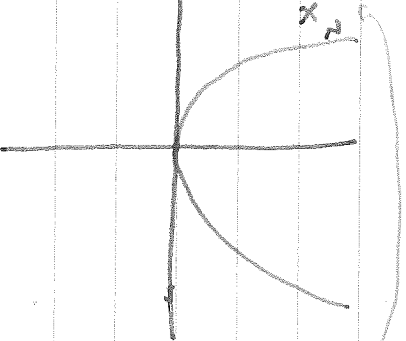
Odd because

$$f(-x) = -x = -f(x) \text{ (analytic)}$$

symm about origin. (Geometric)

Ex: $f(x) = x^2$

EVEN



symm. around y-axis (geometric)

$$f(-x) = (-x)^2 = \overset{1}{(-x)} \cdot \overset{2}{x} = x^2 = f(x) \text{ (analytic)}$$

ODD $f(x) = x^3$

In general, for my power function

EVEN $f(x) = x^n$

$$f(x) = Cx^n \text{ is } \begin{cases} \text{odd if } n \text{ is odd} \\ \text{even if } n \text{ is even} \end{cases}$$

EVEN $f(x) = 1 = 1 \cdot x^0$

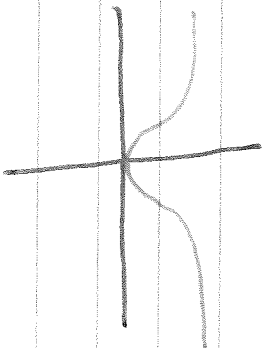
Sums of even functions are even!

$$\begin{aligned} \text{Ex: } x^2 + 2x^4 &\xrightarrow{\text{Plug } (-x)} (-x)^2 + 2(-x)^4 \\ &= (-1)^2 x^2 + 2(-1)^4 x^4 \end{aligned}$$

Sums of odd functions are odd.

$$\text{Ex: } f(x) = \frac{x^2}{1+x^2}$$

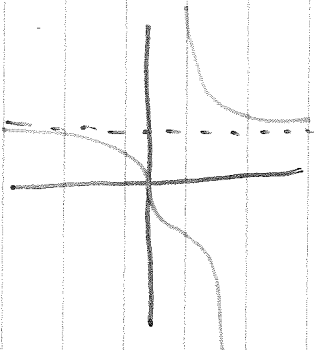
$$f(-x) = \frac{(-x)^2}{1+(-x)^2} = \frac{x^2}{1+x^2}$$



The product/ratio of two even functions is even.

$$\text{Ex: } f(x) = \frac{x^3}{1+x^3}$$

$$f(-x) = \frac{(-x)^3}{1+(-x)^3} = \frac{-x^3}{1-x^3}$$



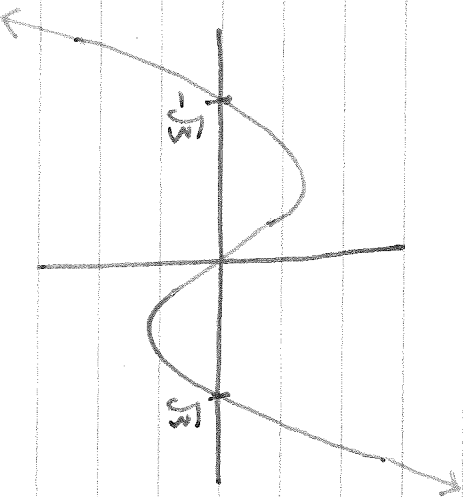
Q: What about the product/ratio of two odd functions?

Graphing simple polynomials

$$\text{Ex: } f(x) = x^3 - 3x$$

When is $x^3 = 3x$?

$$x^2 = 3 \Rightarrow x = \pm\sqrt{3}$$



- Find the zeroes.
- As $x \rightarrow \infty$ or $-\infty$, $x^3 - 3x \approx x^3$
- As $x \rightarrow 0$, $x^3 - 3x \approx -3x$
- Fill the gap

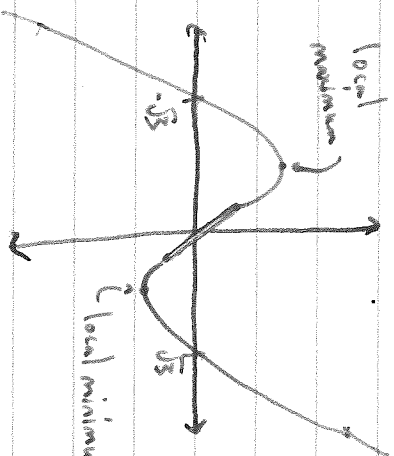
Graphing simple polynomials.

Ex: $f(x) = x^3 - 3x$

Find the roots: $x^3 = 3x$

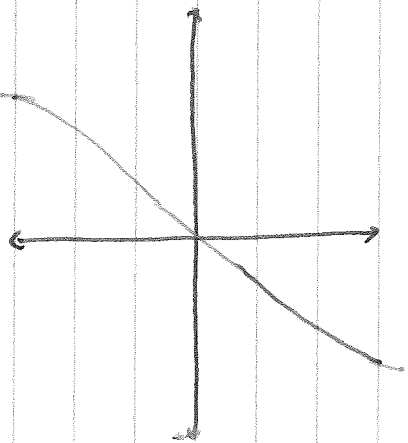
$x^2 = 3$

$x = \sqrt{3}$ or $x = -\sqrt{3}$



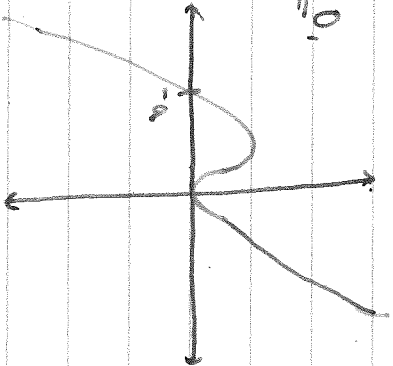
- We know how to graph individual power functions
- We know smaller degrees dominate near $x=0$
- larger degrees dominate as $x \rightarrow \infty$

Ex: $f(x) = x^2 + 3x$



Ex: $f(x) = x^3 + ax^2$

If $a > 0$,



If $a < 0$,

